



# **Nonlinear Aircraft Model**

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# Overview



*Smart Icing Systems Review, September 30, 2002*

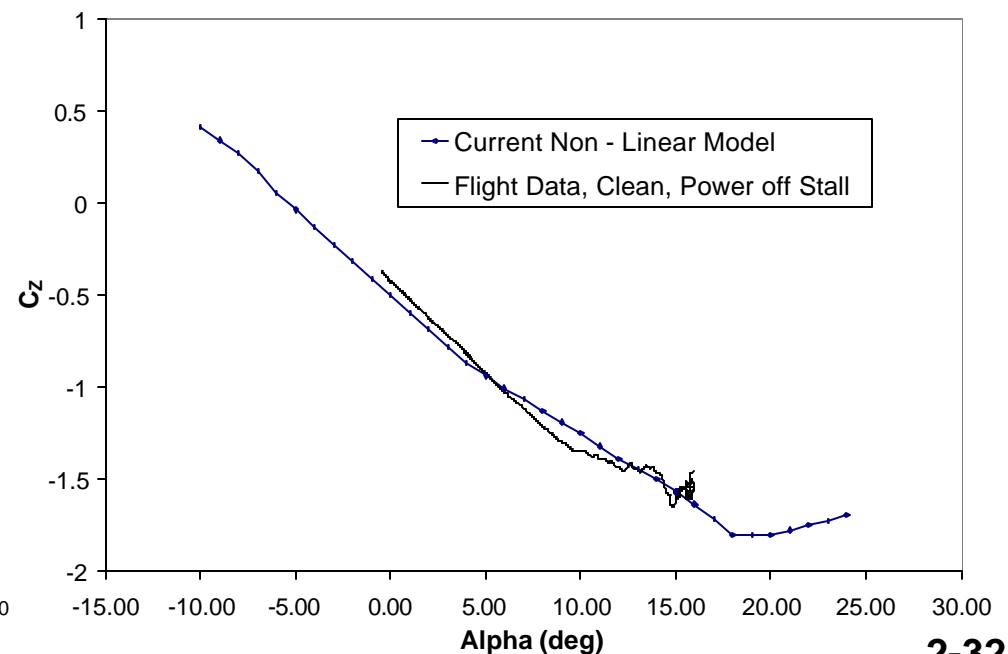
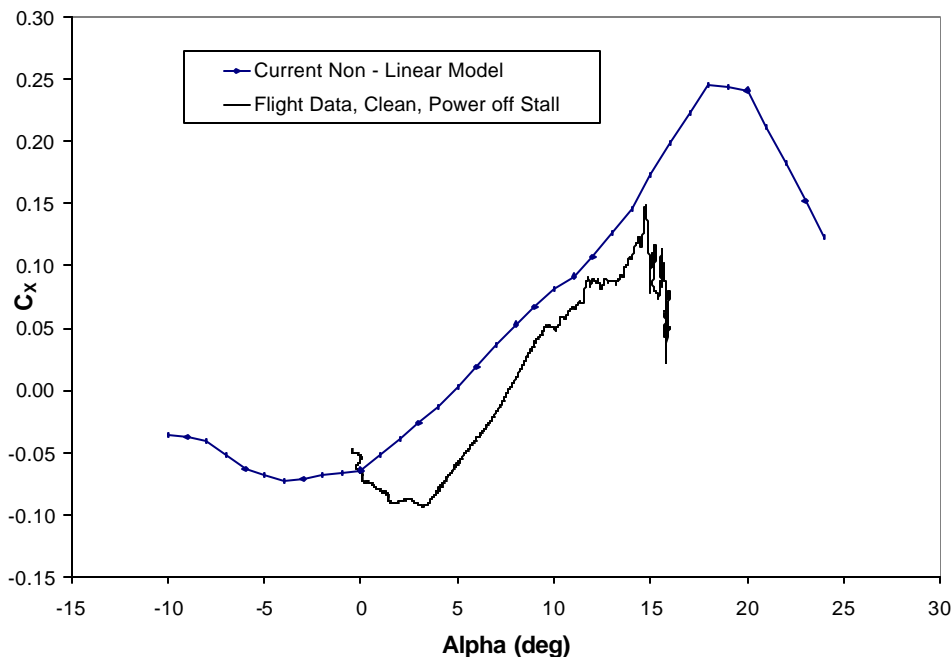
- **Objective:** Non-linear model for all icing conditions, clean, all-ice, wing-ice and tail-ice
- **Motivation:** Simulator  
Envelope Protection  
FDC  
Autopilot  
Characterization
- **Approach:**  $C_L, C_D, C_M = f(\alpha, \delta_e, \eta)$

# The Model



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- Model based on B.A.R. rotary balance test results on the Twin Otter model
- Tests included the clean and a tail iced case of an estimated  $\eta_{ice}$  of 0.08
- Some values manually adjusted to provided a more realistic performance degradation based on Twin Otter flight data,  $\Delta C_{L\alpha}$ ,  $\Delta C_{M\alpha}$  etc



# Model Formulation



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- Extrapolate/Interpolate
- Review of icing severity model

$$C_{A,iced} = (1 + K_{CA} \mathbf{h}) C_{A,clean}$$

## Linear Model

- $C_A$  : Stability and control derivative of interest
- $\eta$  : Icing severity factor
- $K_{CA}$ : Scaling factor for a particular S&C derivative
- For the iced nonlinear model the same basic idea was adopted
- However, changes in the forces and moments were modeled as functions of icing

## Nonlinear Model

- $C_A$  : Force or moment coefficient of interest
- $\eta$  : Icing severity factor
- $K_{CA}$ : Scaling factor for a particular force or moment coefficient

# Model Formulation (cont'd)



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$\Delta C_A$  values from B.A.R. data curve fit as a function of angle of attack and elevator deflection

$$K_{CA} C_{A, clean} = - \frac{\Delta C_A}{h_{ref}}$$

Where  $\eta_{ref}$  is the  $\eta$  value for the B.A.R. data

The non-linear model provides  $K_{CA} C_{A, clean}$  as a function of  $\alpha$  and  $\delta e$  for lift, drag, pitching moment

# Lift Formulation



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Loss in lift due to icing was modeled as a function of the icing severity of the wing

The effect of tail-plane ice on lift was neglected

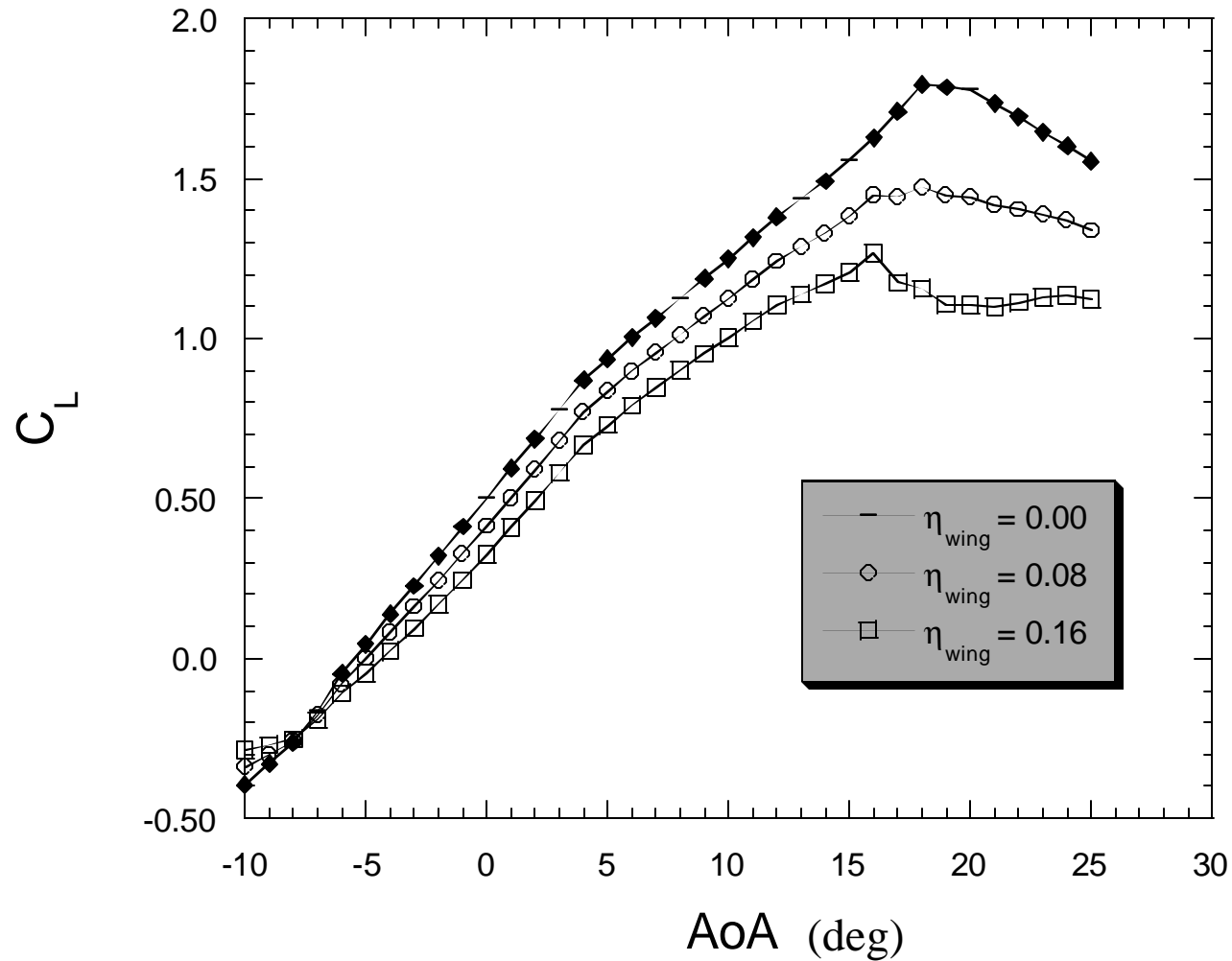
$$C_{L,iced} = C_{L,clean} + \Delta C_L$$

$$C_{L,iced} = C_{L,clean} + K_{C_L} \mathbf{h}_{wing} * C_{L,clean}$$

# Lift Model



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# Drag Formulation



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The drag rise was also modeled as a function of the icing condition of the wing

$$C_{D,iced} = C_{D,clean} + \Delta C_D$$

$$C_{D,iced} = C_{D,clean} + K_{C_D} \mathbf{h}_{wing} * C_{D,clean}$$

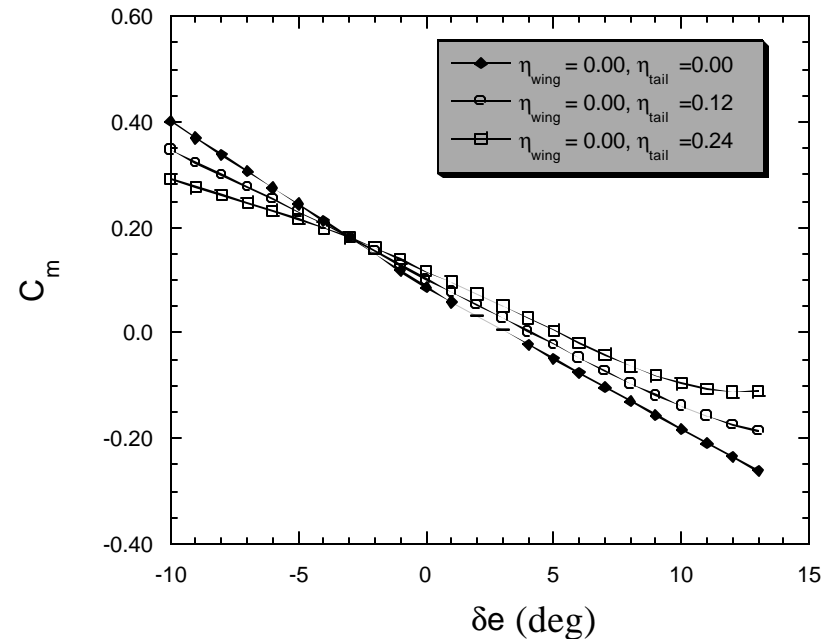
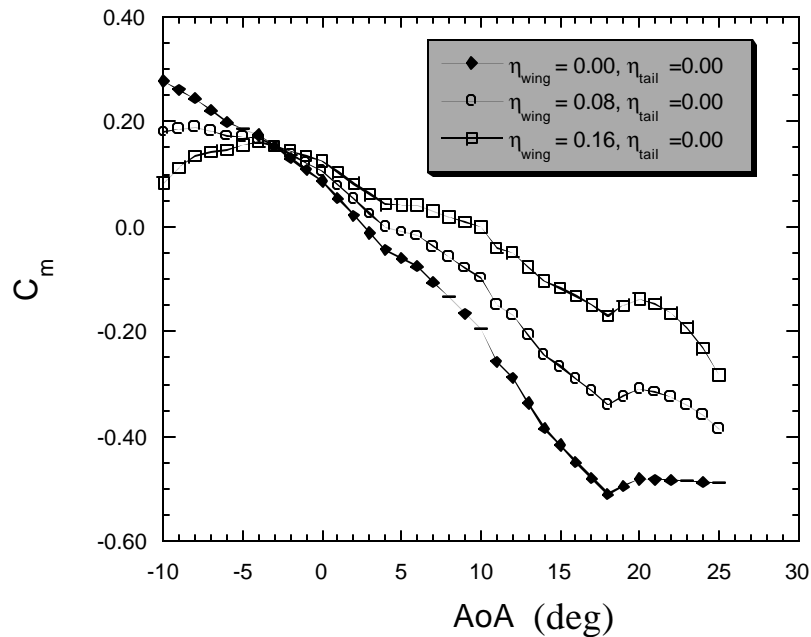
# Pitching Moment Model



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The pitching moment was modeled as a function of both the wing and tail ice

$$C_{m,iced} = C_{m,clean} + K_{Cm,a} h_{wing} * C_{m,clean} + K_{Cm,\partial e} h_{tail} * C_{m,clean}$$



# Work in Progress



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- $\Delta C_l$  (rolling moment) due to differential in the lift generated by left and right wing
- Use different  $\eta$  values on left and right wing to simulate asymmetric icing
- Calculate rolling moment due to different  $\Delta C_L$  values on each wing